CBSE Class 12 Mathematics Formula & Definition Master Sheet (All chapters – full formulas + one-line definitions)

1. Relations and Functions

- Relation: Subset of A×B, describing links between elements.
- Function: Special relation where each element of domain has exactly one image in co-domain.
- Types of relations:
- Reflexive: $(a,a) \in R \ \forall \ a \in A$.
- Symmetric: $(a,b) \in R \Rightarrow (b,a) \in R$.
- Transitive: (a,b), $(b,c) \in R \Rightarrow (a,c) \in R$.
- Equivalence: Reflexive + Symmetric + Transitive.
- Anti-symmetric: (a,b), $(b,a) \in R \Rightarrow a = b$.
- Function types: One-one (injective), onto (surjective), bijective (both invertible).
- Composition: $(f \circ g)(x) = f(g(x))$.
- Inverse function: If f bijective, f^{-1} exists such that $f^{-1}(f(x)) = x$.

2. Inverse Trigonometric Functions

Principal value branch: Domain restricted so inverse trig is single-valued.

Function	Domain	Range
sin ⁻¹ x	[-1,1]	[-π/2, π/2]
cos ⁻¹ x	[-1,1]	[0, π]

tan⁻¹x \mathbb{R} $(-\pi/2, \pi/2)$ cot⁻¹x \mathbb{R} $(0, \pi)$ sec⁻¹x All real no. x such that |x| >= 1 $\left[0, \frac{\pi}{2}\right) U\left(\frac{\pi}{2}, \pi\right]$ cosec⁻¹x All real no. x such that |x| >= 1 $\left[-\pi/2, 0\right) \cup (0, \pi/2]$

Key identities:

- $\sin^{-1}x + \cos^{-1}x = \pi/2$
- $tan^{-1}x + cot^{-1}x = \pi/2$
- $\sec^{-1}x + \csc^{-1}x = \pi/2$
- $tan^{-1}x tan^{-1}y = tan^{-1}((x-y)/(1+xy))$ (adjust for quadrant)

3. Matrices

- Matrix: Rectangular array of numbers, order m×n.
- Special matrices: zero, identity I_n , diagonal, scalar, symmetric $A^t=A$, skew-symmetric $A^t=-A$.
- Operations:
- $(A+B) = [a_{ij} + b_{ij}]$
- Scalar × A: multiply each entry.
- Multiplication: (AB)_{ij} = $\sum a_i k b_{kj}$ (m×p with p×n results in m×n).