

Section A: MCQs (20 questions, single-correct)

1. If $S = \{z \in \mathbb{C} : |z-2+3i| = 5\}$, then the locus of z in the Argand plane is
 - A) Circle, center $(2,-3)$, radius 5
 - B) Circle, center $(2,3)$, radius 5
 - C) Line $x+3y=5$
 - D) Parabola with focus $(2,3)$
2. The domain of $f(x)=\ln(2-\sqrt{x-1})$ is
 - A) $(-\infty,1]$
 - B) $[1,(-\infty,2]$
 - C) $(1,2]$
3. If a,b,c are in AP and $a+b+c=15$, $b-a=3$, then c equals
 - A) 3 B) 6 C) 9 D) 12
4. Let $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$. Then for any $n \in \mathbb{N}$, $\det(A^n)$ equals
5. The value of $\lim_{x \rightarrow 0} \frac{\sin(3x)-3x}{(x^3)}$ is
 - A) $-9/2$ B) 0 C) -9 D) $-27/2$
6. If $y=x^x$ for $x>0$, then dy/dx at $x=1$ equals
 - A) 1 B) e C) $1+\ln 1$ D) $1+\ln 1/e$
7. Tangent to the curve $y=\ln(x+\sqrt{x^2+1})$ at $x=0$ has slope
 - A) 0 B) 1 C) -1 D) $1/2$
8. $\int (x e^x) dx$ equals
 - A) $x e^x + C$
 - B) $(x-1)e^x + C$
 - C) $(x+1)e^x + C$
 - D) $e^x + C$
9. Area bounded by $y=|x|$ and $y=2$ is